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Integration

Lebesgue Integration H. Vic Dannon

Abstract:

We show that

- 1. the Riemann integral may exist when the Lebesgue integral does not
- 2. the Fundamental Theorem of Calculus may hold for Riemannian Integration but not for Lebesgue integration of the same function
- 3. The same limit function of Integrable functions may be Riemann-Integrable but not Lebesgue integrable.

Therefore, contrary to Common belief, Riemann Integration is more general than Lebesgue Integration.

Furthermore, we show that a convergent sequence of measurable functions may have a non-measurable limit function.

This cast a doubt on the validity of the main results of Lebesgue theory.

Consequently, Riemannian Integration is not only a superior Integration Theory. It is the only Integration Theory that we have.

<u>Riemannian Integration</u> H. Vic Dannon

Abstract: Riemann's Theory of Integration appeared in Riemann's paper "On the Representation of a Function by a Trigonometric Series".

There, Riemann

- 1. presents his Oscillation Conditions for integrability,
- 2. establishes the integrability of his example of a series of functions with infinitely many discontinuities in any interval of real numbers, and
- 3. obtains a sequence of necessary and sufficient conditions for the integration of a singular function.

These fundamental results constitute the Riemannian Integration Theory that we present here

In a forthcoming article, we show that Infinitesimal Calculus allows integration of functions that are not Riemann Integrable.

Keywords: Riemann, Integration, Integrability, Oscillation, Discontinuity, Singularity,

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